

# Thermal Modeling In Support of Exposure Limits Above 6 GHz

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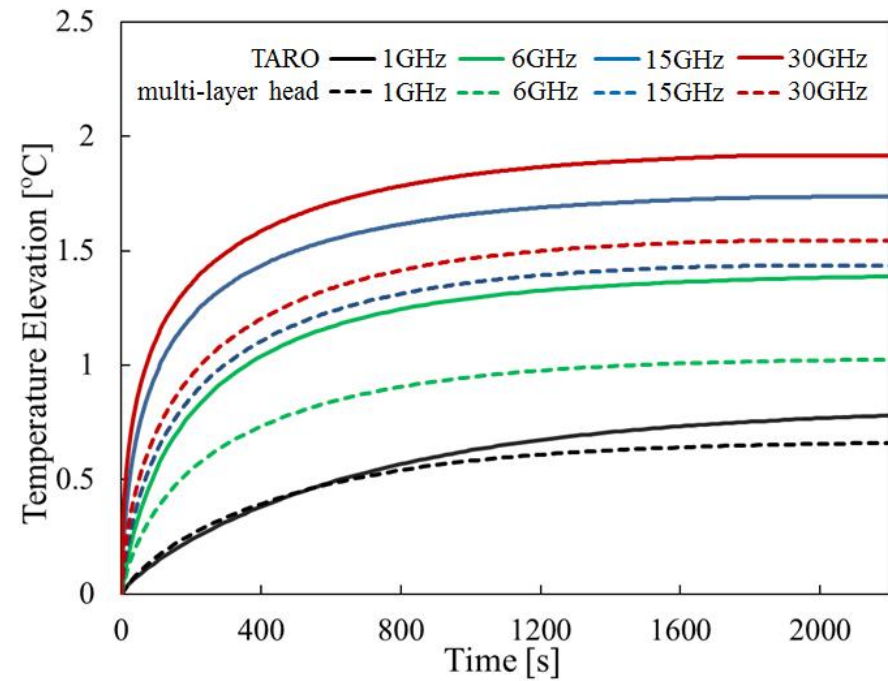
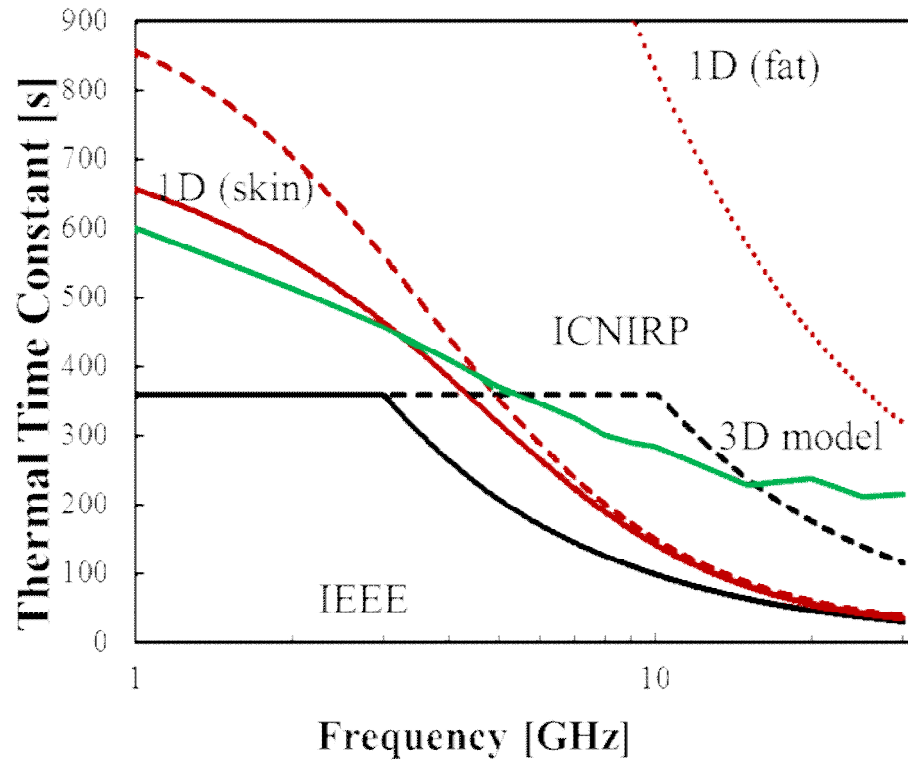
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(presented by A. Hirata)



# Results in Hirata Lab



# Goal of Work:

- Estimate exposure conditions  $>$  “transition” that are below thresholds for thermal hazard
- Use simple theory to develop scaling relations
- Develop Green’s function approach to define averaging times and areas
- Complement more detailed thermal models (Hirata’s group)



# Penne's Bioheat Equation

In simplified form, Pennes' bioheat equation (BHTE) can be written:

$$k\nabla^2 T - \rho^2 C m_b T + \rho SAR = \rho C \frac{dT}{dt} \quad (1)$$

where

T is the temperature rise of the tissue (°C) above the baseline temperature (i.e. temperature above that previous to RF exposure)

k is the thermal conductivity of tissue (0.37 W/m °C)

SAR is the microwave power deposition rate (W/kg)

C is the heat capacity of the tissue (3390 W sec/kg°C)

$\rho$  is the tissue density (1109 kg/m<sup>3</sup>)

and  $m_b$  is the volumetric perfusion rate of blood ( $1.767 \cdot 10^{-6}$  m<sup>3</sup>/(kg sec) or 106 ml/min/kg in the mixed units typically used in the physiology literature).



# Scaling Properties of BHTE

$$\tau_1 = l / m_b \rho \approx 500 \text{ sec}$$

time constant for heat removal by blood flow

$$\tau_2 = L^2 / \alpha$$

Thermal diffusion

$$R_1 = \frac{\sqrt{k}}{r \sqrt{m_b c}} \gg 7 \text{ mm}$$

Screening distance by blood flow

$$R_2 = \sqrt{4\alpha t} \gg 0.5\sqrt{t} \text{ mm}$$

By thermal diffusion



## Approximation 1 – Pure Surface Heating

- Excellent approximation **>30 GHz**
- Decent approximation (conservative) 10-30 GHz
- Yields simple expression for rise in surface temperature:

$$T_{sur}(t) = \frac{I_0 T_{tr}}{r \sqrt{km_b C}} \operatorname{erf} \left( \sqrt{\frac{t}{t_1}} \right) = \frac{I_0 T_{tr} R_1}{k}$$

$$= 0.019 I_0 T_{tr} \operatorname{erf}(\sqrt{t / t_1})$$

(Takes » 500 sec to reach steady state, independent of frequency)



## Approximation 2 – Conduction Only Model

- Excellent approximation for small exposed areas and short times
- Yields simple expressions for transient rise in surface temperature and for small exposed areas :

$$T^{ss} = \frac{I_o T_{tr} R_1}{k} (1 - e^{-x})$$

where  $x = R_0 / R_1$ .

Local heating – independent of blood flow

$$T_{sur}(t) \gg 10^{-3} I_o T_{tr} \sqrt{t} \text{ } ^\circ\text{C}$$

Transient heating proportional to  $t^{1/2}$

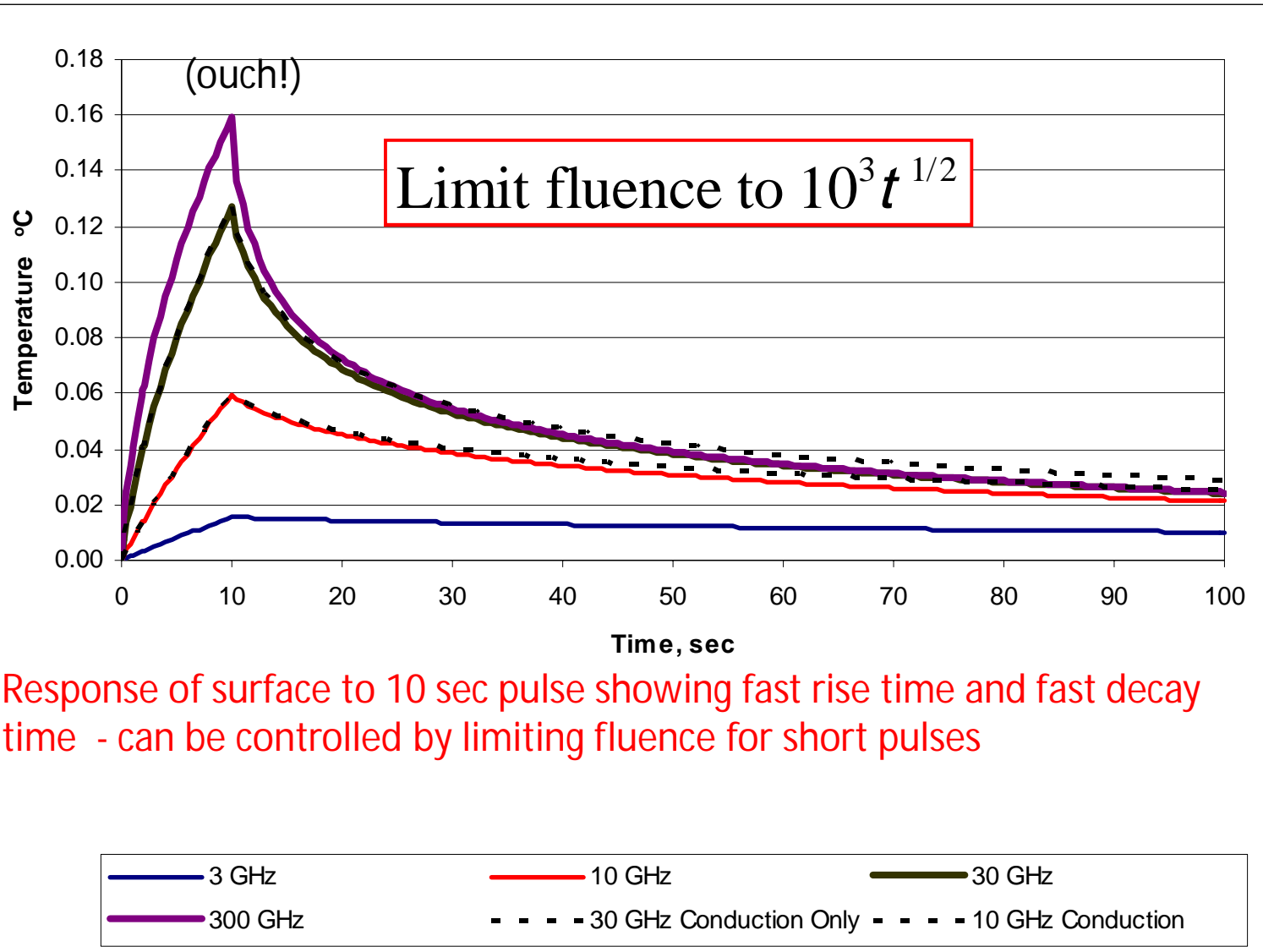


# Implications for Guidelines

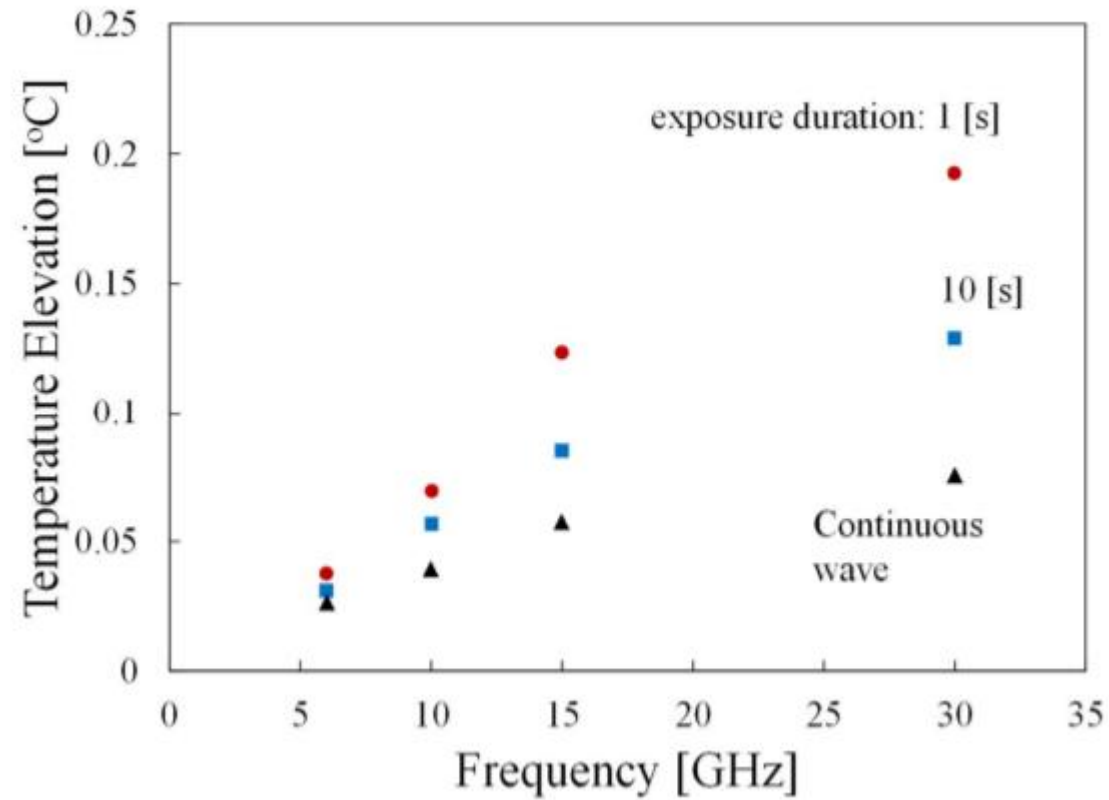
- Present IEEE, ICNIRP guidelines are **excessively conservative** above transition frequency.  
Predicted skin temp. increases » 0.1 °C
- “Averaging times” are **far too short** at mm wave frequencies, should be several hundred seconds
- **Need new provisions** for short high intensity pulses that can create damage before victim can withdraw (“Active Denial type pulses”)







## Results in Hirata Lab



# Other comments

- Emphasis on steady state temperature is **not correct**. Few people will sit motionless while their skin temperature creeps above threshold for pain then stay longer until burns occur
- Main prospective cause of thermal injury – **high exposures that cause damage before victim can escape**
- **Second concern: vulnerable individuals with impaired thermal pain sensation**



Personal electronic devices such as laptop computers and transmitters used near the body have similar risk profiles (for thermal hazards)

For such devices, might want to frame limits  $> 10$  GHz as upper bound to skin temperature, not MPE.

This would avoid uncertainties in calculating temperature from incident power density – just measure skin temperature directly

e.g. IEC 60601-1:2015 specifies limits for “touch temperature” for devices that will be in contact the body.



# Thermal Response of Human Skin to Microwave Energy: A Critical Review

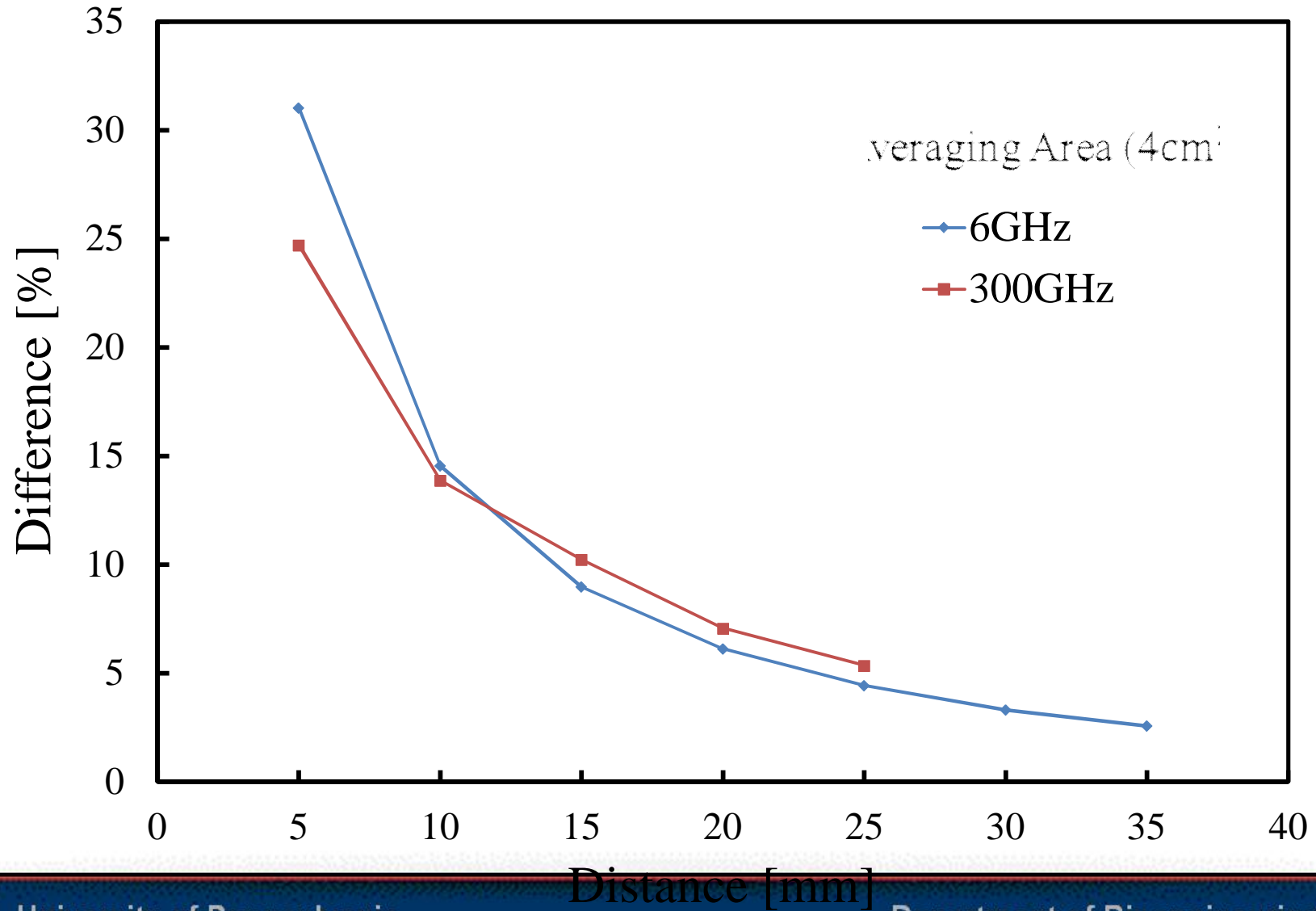
Kenneth R. Foster,\* Marvin C. Ziskin,† and Quirino Balzano‡

**Health Phys. 111(6):528–541; 2016**

Thermal Modeling for the Next Generation of Radiofrequency Exposure Limits: Comment  
Kenneth R. Foster\*, Marvin C. Ziskin+, and Quirino Balzano++  
(under review with Health Physics)



Difference rate between  $S_x$  and  $S_{xyz}$  due to Dipole Antenna  $\frac{S_{xyz} - S_x}{S_{xyz}} \times 100$  (%)



### Heating factor in the homogeneous model emitted from plane wave)

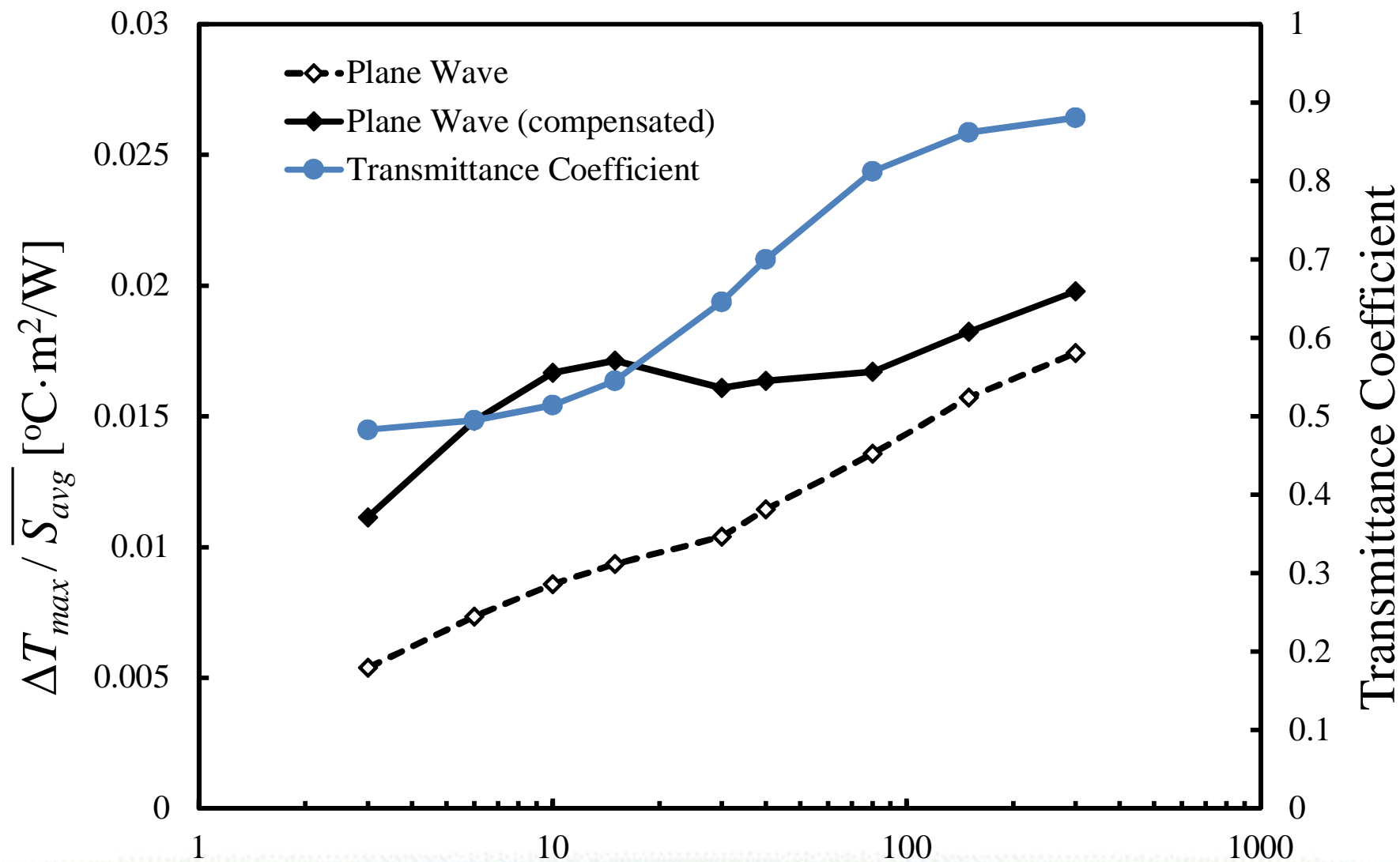
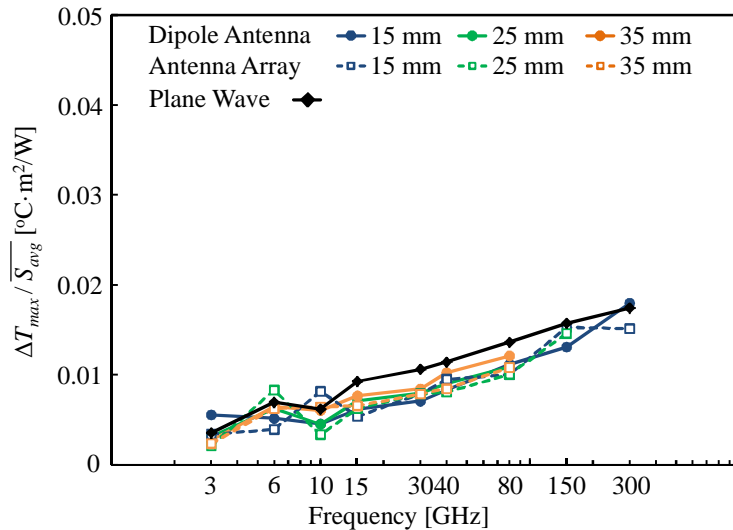
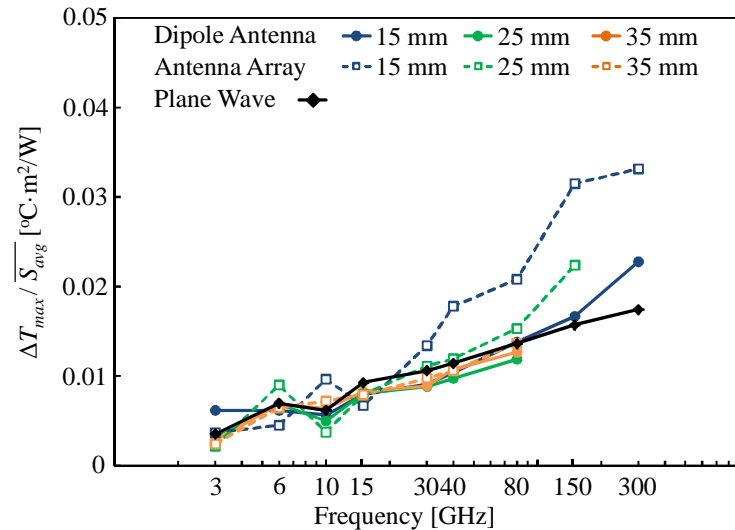


Fig.5

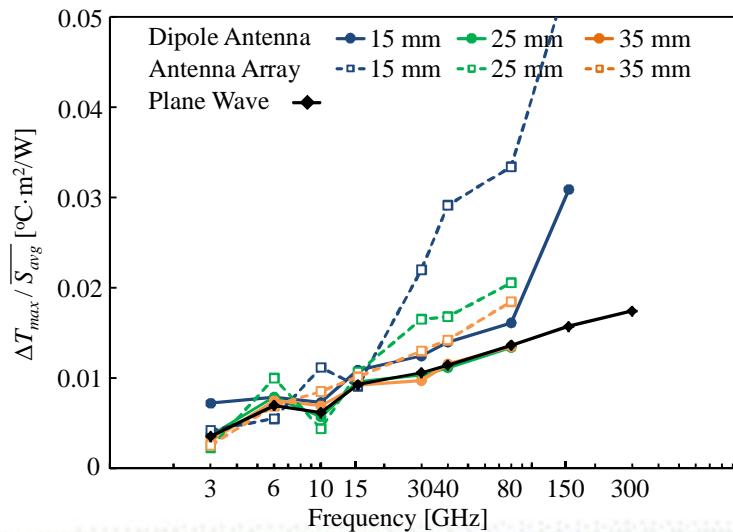
### Heating Factor (Ratio of Max. Temperature elevation to Avg. Power Density)



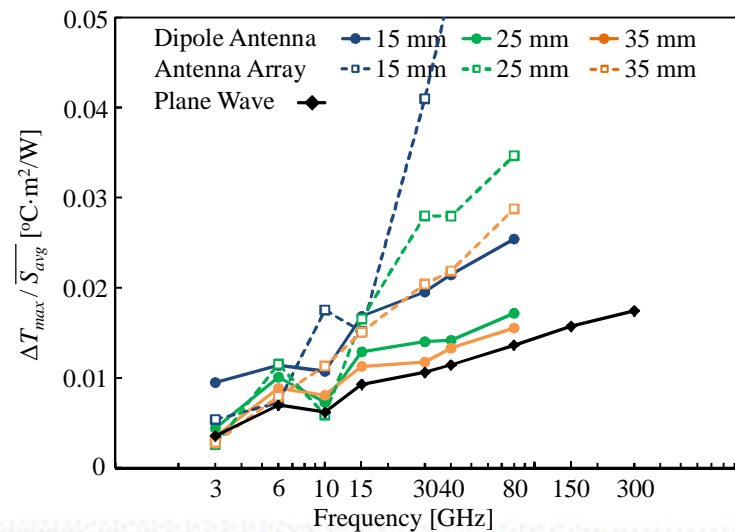
(a)



(b)



(c)



(d)

