

(Thermal) mechanisms of interaction between HF and biological systems

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Int. J. Hyperthermia, June 2011; 27(4): 307–319

REVIEW ARTICLE

**Thermal aspects of exposure to radiofrequency energy:
Report of a workshop**

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Mechanism” is defined by IEEE (2006) as a theoretical formulation that:

- can be used to **predict** a biological effect in humans;
- can be **formulated** in an explicit model using equations or parametric relationships;
- is **supported by data** from humans, or by animal data and can be extrapolated confidently to humans;
- is supported by **strong evidence**; and
- is **widely accepted** among experts in the scientific community.



Mechanism 1

(metric: temperature increase)

Thermal Dependence of Biological Processes



Arrhenius' equation

$$k = Ae^{-E_a/(RT)}$$

k = rate constant of a chemical reaction

T = absolute temperature (in K)

A = pre-exponential factor (or simply the prefactor),

T

E_a = activation energy

R = universal gas constant

R

For most biological systems, $Q_{10} \sim 2$ to 3



Q_{10} - Practical characterization of temperature dependence

$$Q_{10} = \left(\frac{R_2}{R_1} \right)^{10/(T_2 - T_1)}$$

where

R is the rate

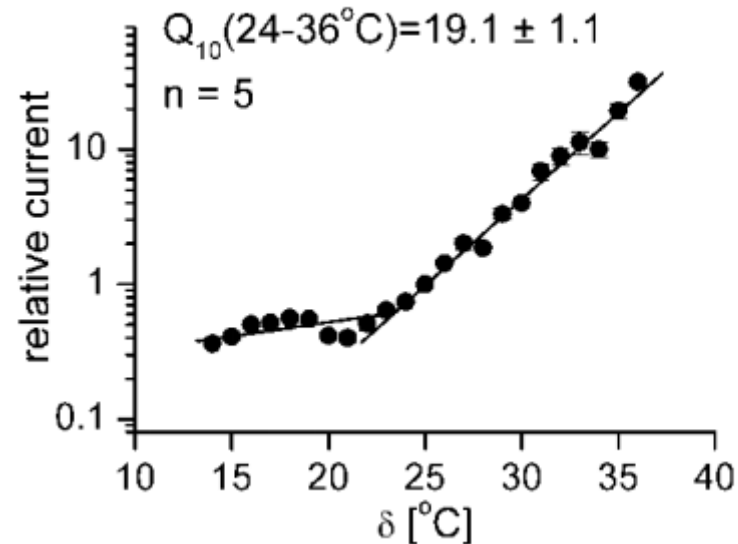
T is the temperature in Celsius degrees or kelvins.

Q_{10} of 2 means that a 10°C increase in temperature doubles the reaction rate

Typical range 1.5-3



More sensitive systems exist:



Membrane conductance of TRPV4 channels

“TRPV4 is a functional temperature-sensing channel in native endothelium”

(Watanabe, Hiroyuki, et al. "Heat-evoked activation of TRPV4 channels in a HEK293 cell expression system and in native mouse aorta endothelial cells." *Journal of Biological Chemistry* 277.49 (2002): 47044-47051.)



Fun Fact

de Pomerai et al. (2000, 2006) reported induction of heat shock proteins in the nematode *C. elegans* after extended (2 to 24 h) exposures to microwave energy.

This effect was eventually found to be associated with a small (0.2°C) temperature increase in the irradiated samples (de Pomerai et al. 2006).



Relevance to Exposure Guidelines

- Arrhenius equation says that *any* temperature change will produce biological effects
 - some may be adaptive or not adverse to health
 - Some reported “nonthermal” effects might be thermally induced after all
- But... difficult to extrapolate to low exposures (no data)



Mechanism 2

(metric: temperature increase)

Thermal Damage

$$\frac{d\Omega}{dt} = A \exp\left(\frac{-E_a}{R_b T(t)}\right) \quad \Omega = \int_0^t A \exp\left(\frac{-E_a}{R_b T(t)}\right) dt$$

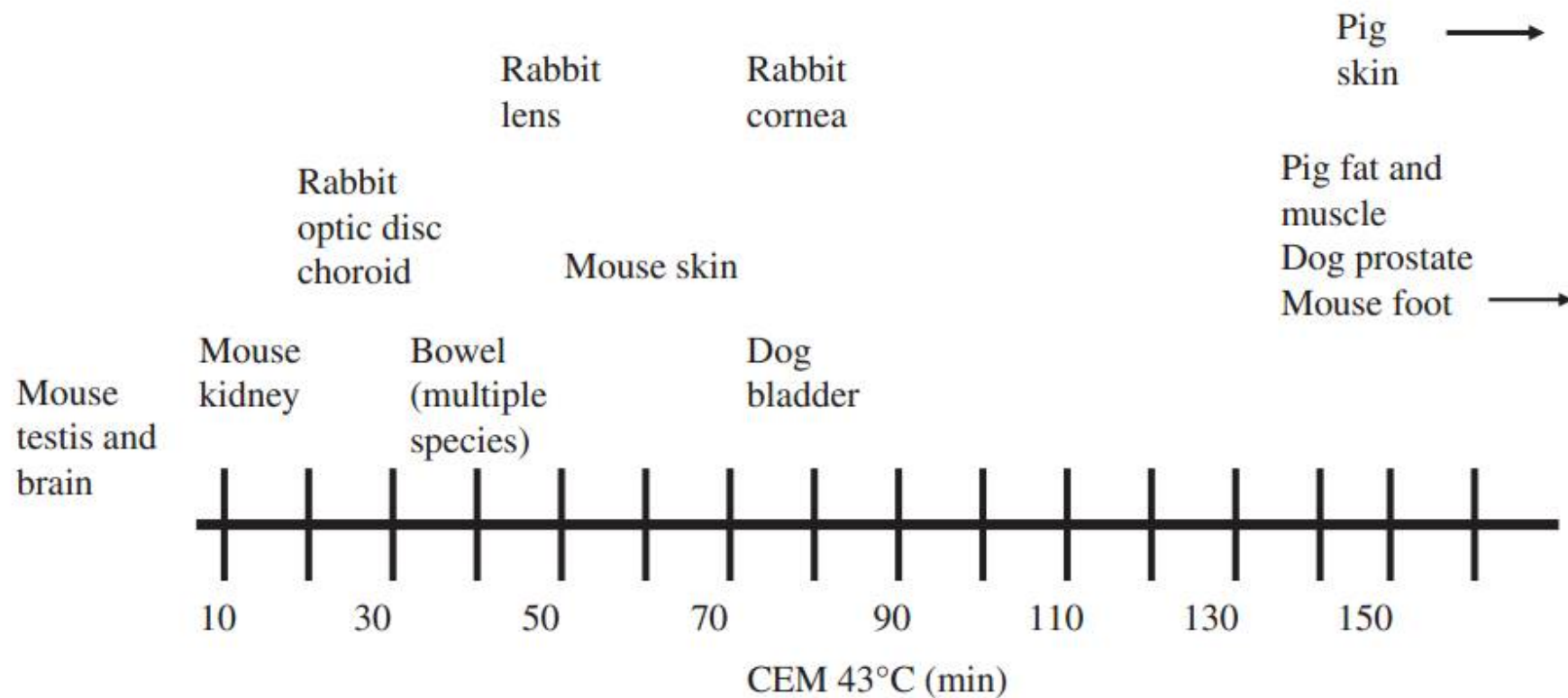
Ω is the thermal damage index

isoeffect dose cumulative equivalent min 43 (CEM43)

$$CEM43 = \Delta t R^{43-T_c}$$

$$\begin{aligned} R &= 0.25 \text{ for } T < 43 \text{ C} \\ &= 0.5 \text{ for } T > 43 \text{ C} \end{aligned}$$

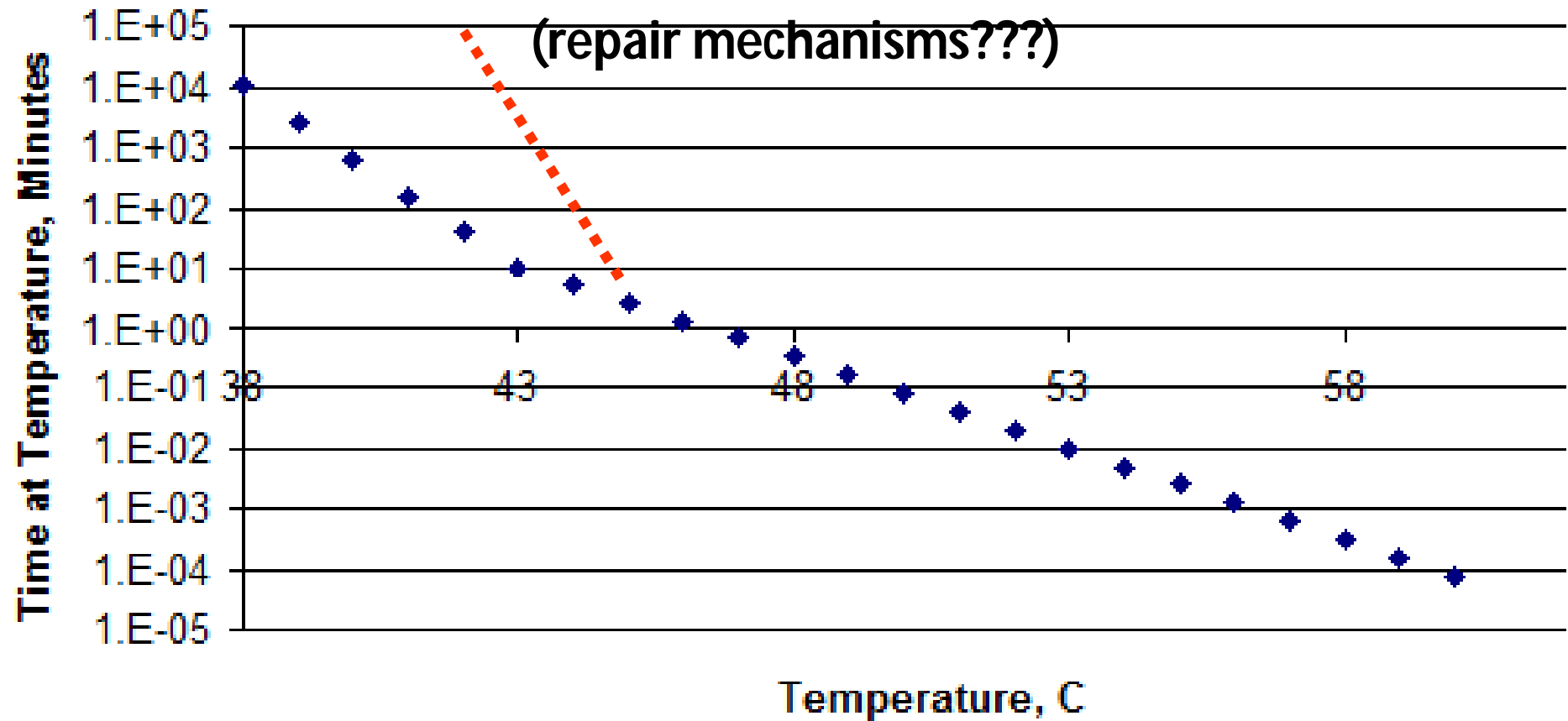




proximate ranking of thresholds for thermal damage of various tissues. Adapted from a figure c



Exposure Time (CEM43=10)



Fun Fact

Tissues can sustain high temperature increases for short time periods



(COURTESY USMC)



Gaps in Knowledge

- Data for thermal injury very scattered, not collected using consistent protocols
- Most data at thermal exposures far above safety limits
- Little (no?) basis to extrapolate to low thermal exposures.

Relevance to Guidelines

Nil unless limits are raised considerably



Mechanism 3

(metric: time rate of change of temperature)

Microwave Auditory Effect/Thermoelastic expansion

$$P_o = \frac{c_s \beta R \rho S}{C J}$$

P_o = sound pressure

R is the diameter of the heated region

S is the SAR in the exposed region,

β = volumetric thermal expansion coefficient of the tissue, c = velocity of sound

C is the heat capacity of the tissue, and J is the mechanical equivalent of heat.



Microwave auditory effect

- Typical pulse intensity W/cm^2 , μs pulses

Implications for Guidelines

Threshold hearing phenomenon - no apparent hazard.

Might be considered as an annoyance



Mechanism 4

(metric: time rate of change of temperature)

Thermally-induced membrane depolarization

High dT/dt will affect membrane activity (Wachtel)

Very high peak SAR's needed (tens of W/kg)

Not relevant to exposure limits



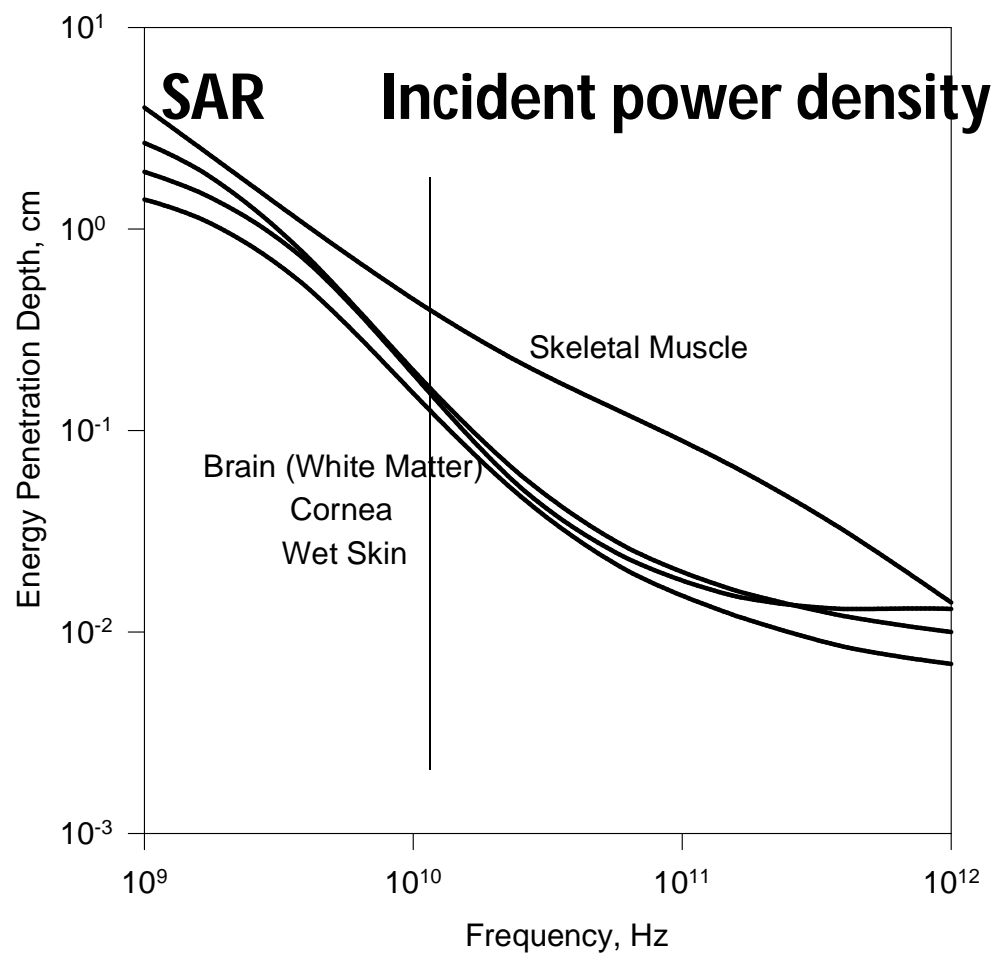
Thermal and Spatial Averaging

WHENCE 6 MINUTES?

“Our early C-95.4 Committee needed to recommend a time constant. My suggestion was 0.1 h. I was trying to come up with a number with as few significant figures as I could, considering the precision of what we were dealing with. A minute was too short — an hour was too long. But, alas, 0.1 h turned into 6 min, and 6 min implies an accuracy beyond the art...”

Tom Ely (1998) quoted in Foster et al, Bioelectromagnetics 19:420 – 428 (1998)





Heating of Tissues by Microwaves: A Model Analysis

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Pennes' Bioheat Equation (1948)

Heat conduction
Blood flow

$$k\nabla^2 T - \rho_b \rho_t C_b m_b T + \rho_t SAR = C_t \rho_t \frac{\partial T}{\partial t}$$

T = tissue temperature

k = thermal conductivity of tissue (0.4 W/m °C)

SAR = microwave power deposition rate (W/kg)

C_b = heat capacity of blood (4000 W sec/kg°C)

C_t = heat capacity of tissue (4000 W sec/kg°C)

D_b = density of blood (1000 kg/m³)

D_t = density of tissue (1000 kg/m³)

m_b = volumetric perfusion rate of blood

(40 mL/100 g of tissue per min)



Limiting solutions to BHTE

Early transient period (heat storage term dominates)

$$\left. \frac{dT}{dt} \right)_0 = SAR / C_t$$

Steady state (convection term dominates)

$$T_{ss} = \frac{SAR}{\rho m_b C} + \frac{k \nabla^2 T}{\rho_b \rho_t C_b m_b}$$

↑ Usually smaller term



Two Time Scales in Bioheat Equation

$$\tau_1 = \frac{1}{m_b \rho} \approx 60 \text{ sec (convection)}$$

$$\tau_2 = \frac{\rho CL^2}{k} \approx 800 \text{ sec (diffusion, for } L = 1 \text{ cm)}$$
$$\approx 8 \text{ sec (diffusion, for } L = 1 \text{ mm)}$$

**Shorter
time
constant
dominates**

m_b = blood flow

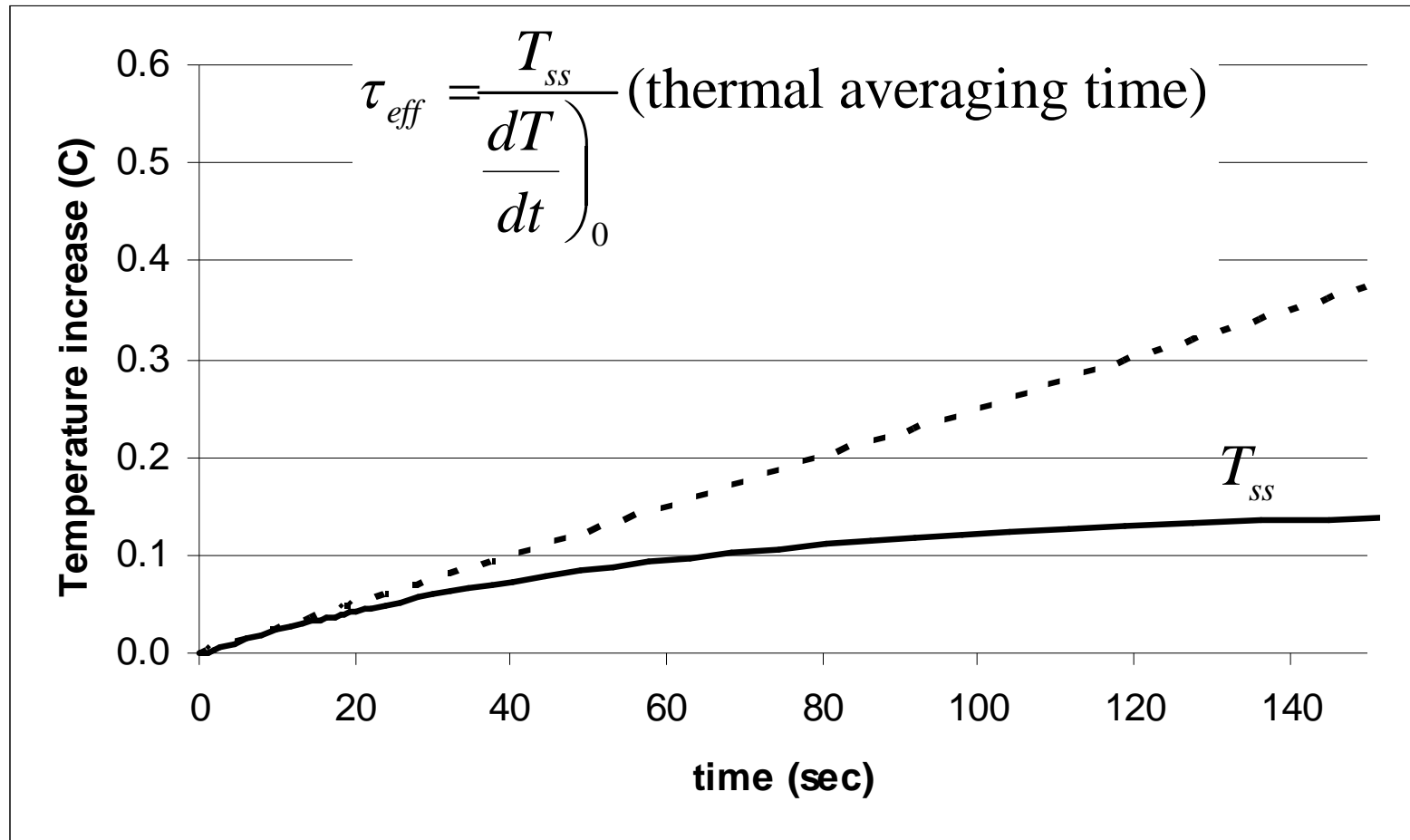
ρ = tissue density

k = thermal conductivity of tissue

L = distance scale of heating (SAR)

C = specific heat of tissue





Green's function for BHTE

Steady-state spherical

$$G(R) = \frac{\rho_t}{4\pi k_t R} e^{-R/R_{conv}}$$
$$R_{conv} = \frac{\sqrt{k_t}}{\rho \sqrt{m_b c}} \approx 1 - 2 \text{ cm}$$

R = distance from center of source

R_{conv} = distance scale for convection

ρ_t = tissue density

k_t = thermal conductivity of tissue

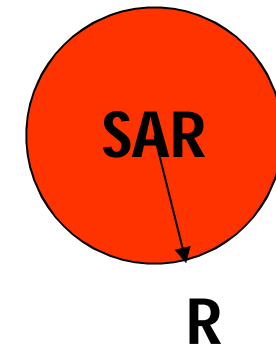
c = specific heat of tissue

m_b = blood perfusion rate



Thermal Response Time and Steady State Temp. Increase in Heated Tissue Sphere (heat conduction only)

Radius	Thermal relaxation time, sec	Maximum steady-state temperature increase above surrounding medium, °C (SAR 10 W/kg)
1 nm	3.5 ps	$8 \cdot 10^{-15}$
10 nm	0.35 ns	$8 \cdot 10^{-13}$
1 μm	3.5 μs	$8 \cdot 10^{-9}$
1 mm	3.5 s	0.008
1 cm	350 s	0.8



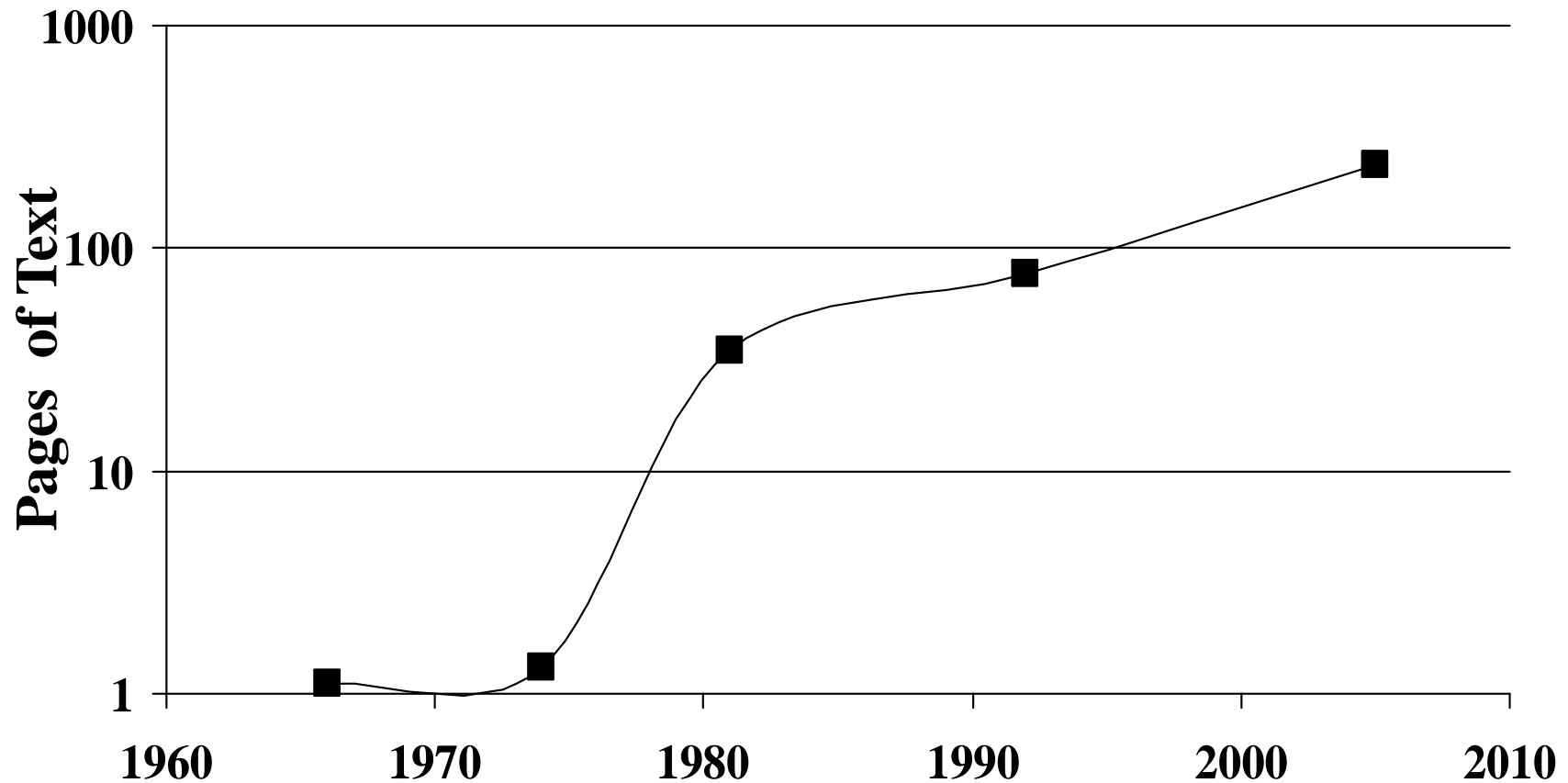
Bottom Line

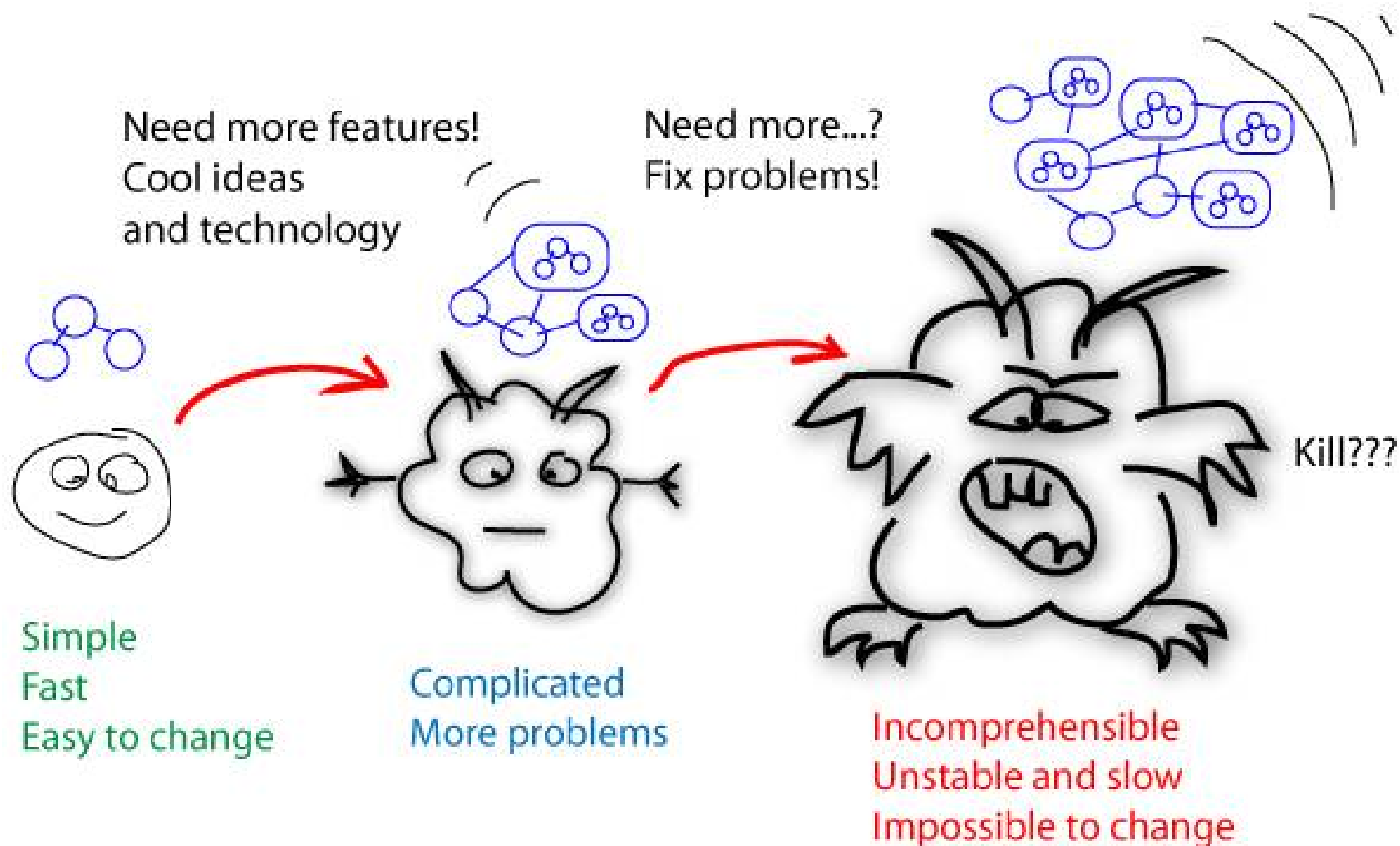
- Averaging distance is \approx 1-2 cm (steady state heating)
Thermal conduction is nature's way of averaging thermal exposure
- Useful definition of averaging time: steady state temperature increase/ peak SAR

How much precision is needed and at what cost in complexity?



Does ANSI C95.1 Follow Moore's Law?





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